

# **Modeling and Forecasting Exchange Rate Volatility and it's Impact on Pakistan's Economy**



By

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2016**



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بِسْمِ اللّٰهِ الرَّحْمٰنِ الرَّحِيْمِ

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BY  
**MUHAMMAD FAIZAN**

*A dissertation*  
*Submitted in the partial fulfillment of the*  
*Requirements for the degree of*  
**MASTER OF SCIENCE**  
**IN**  
**STATISTICS**

SUPERVISED BY:

***Dr. Zahid Iqbal***

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**Faculty of Basic and Applied Sciences**  
**International Islamic University, Islamabad**  
**Pakistan**  
**2016**

## Certificate

### **Modeling and Forecasting Exchange Rate Volatility and its Impact on Pakistan's Economy**

By

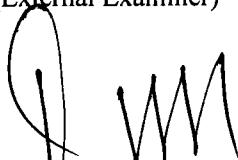
***Muhammad Faizan***

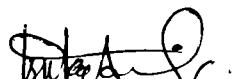
A DISSERTATION SUBMITTED IN THE PARTIAL FULFILLMENT OF THE  
REQUIREMENTS FOR THE DEGREE OF THE MS IN STATISTICS

We accept this dissertation as conforming to the required standard.

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**2016**

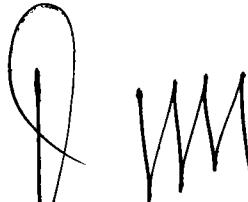
*For My Worthy Parents*

*Thank you for allowing me to follow my heart and  
encouraging me to pursue my dreams.*

## **Forwarding Sheet by Research Supervisor**

The thesis entitled "Modeling and Forecasting Exchange Rate Volatility and it's Impact on Pakistan's Economy" submitted by Muhammad Faizan, Registration No: 25-FBAS/MSST/S-13, in partial fulfillment of MS degree in Statistics has been completed under my guidance and supervision. I am satisfied with the quality of his research work and allow him to submit this thesis for further process to graduate with Master of Science Degree from Department of Mathematics and Statistics, as per IIU Islamabad rules and regulations.

Dated \_\_\_\_\_



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**MUHAMMAD FAIZAN**

## **DECLARATION**

I, **Muhammad Faizan**, hereby declare that this dissertation is original and has never been presented in any other institution. I, moreover, declare that any secondary information used in this dissertation has been duly acknowledged.

Signature: \_\_\_\_\_

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## **LIST OF ABBREVIATIONS**

ACF- Auto Correlation Function

AIC - Akaike Information Criteria

SIC – Schwartz information Criteria

ADF - Augmented Dickey-Fuller

AR - Auto Regressive

ARCH - Auto Regressive Conditional Heteroscedasticity

ARIMA - Auto Regressive Integrated Moving Average

EGARCH - Exponential Generalized Auto Regressive Conditional Heteroscedasticity

GARCH - Generalized Auto Regressive Conditional Heteroscedasticity

GED - Generalized Error Distribution

GNP - Gross National Product

MA - Moving Average

MAE - Mean Absolute Error

MAPE - Mean Absolute Percentage Error

PAC - Partial Auto Correlation

PACF - Partial Auto Correlation Function

RMSE - Root Mean Square Error

USD - United States Dollar

GDP – Gross Domestic Product

FDI – Foreign Direct Investment

REM – Remittances

INF - Inflation Rate

VAR – Vector autoregressive

## ABSTRACT

This dissertation describe an empirical study of modeling and forecasting time series data of Exchange rate and it's impact on Pakistan's economy. The modeling and forecasting of exchange rate and its volatility has important implications for macro-economic decisions making. This research is divided into two parts, at first part the study aims to capture volatility patterns using different time series models. Monthly and yearly exchange rate of Pakistan to USD for the period ranging 1981 to 2014 obtained from State Bank of Pakistan. We have ran AR (Autoregressive), MA (Moving Average) and different combination of both ARIMA (Autoregressive Integrated Moving Average) models. The diagnostic checking has shown that ARIMA (3,1,2) and ARIMA (1,1,2) [on the basis of Akaike Information Criteria (AIC) and Schwartz Information Criteria (SIC)] are appropriate models for monthly and yearly Exchange rate returns, respectively. ARIMA (3,1,2) and ARIMA (1,1,2) selected, amongst different sets of AR (Autoregressive), MA (Moving Averages) and ARIMA, as Mean models for further applying ARCH family of models. For diagnostic checking we also performed forecast from 1981 to 2014 as well as 2010 to 2014 with the help of these selected models. The performance of forecast was evaluated by RMSE (Root Mean Square Error), MAE (Mean Absolute Error), MAPE (Mean Absolute Percentage Error) and Theil's Inequality coefficient. The ARCH-LM test and residual of ARIMA (3,1,2) and ARIMA (1,1,2) have justified to run ARCH family of models.

Similarly, for capturing the volatility of Exchange Rate returns, used ARCH family of model i.e. Autoregressive conditional heteroscedasticity (ARCH), Generalized Autoregressive conditional heteroscedasticity (GARCH), Integrated Generalized

Autoregressive conditional heteroscedasticity (IGARCH) and Exponential Generalized Autoregressive conditional heteroscedasticity (EGARCH). After running the different sets of ARCH, GARCH, EGARCH, IGARCH. The diagnostic checking has shown that for monthly exchange rate data the ARIMA(3,1,2)-EGARCH (1,1) and for yearly exchange rate data the ARIMA(1,1,2)-EGARCH(1,1) are the best fitted models for modeling and forecasting Exchange Rate volatility. We have made forecast from 1981 to 2020 with these models. The performance of forecast was evaluated by RMSE (Root Mean Square Error), MAE (Mean Absolute Error), MAPE (Mean Absolute Percentage Error) and Theil's Inequality coefficient. These forecasts would be helpful for the policy makers to foresee the future requirements. Monthly and Yearly Exchange Rate data (PKR/Us-Dollar) is obtained from the State Bank of Pakistan (SBP).

The second part of this study was designed to investigate the effect of Exchange Rate's volatility on the Real Gross Domestic Product (GDP) of Pakistan. The study has used six variables, the data for the variables i.e. Inflation Rate (INF), Foreign Direct Investment (FDI), Exports, Real GDP and Foreign Remittances obtained from The State Bank of Pakistan. The empirical relationship between exchange rate volatility and Real Gross Domestic Product (GDP) have been found while employing an econometric study based on Vector Autoregressive (VAR) methodology for yearly data collected from 1981 to 2014. We have also used the Vector Autoregressive (VAR) model to estimate the Impulse Response functions and Variance Decompositions for Gross Domestic Product in order to determine how Exchange Rate shock effects Real GDP. in short run the Real GDP account for 67.32% variation of the fluctuation in Real GDP (own shock) and in long run i.e. 10 years is 32.32% variation of the fluctuation in Real GDP (own shocks). Shock to Exchange rate can cause 2.63% in short run but contribution in long run is 7.76% to the Real GDP in Pakistan. Impulse response shows due to exchange rate shocks, GDP

Changes negatively in the short run but after that it steadily change in positive direction for the effects of one standard deviation in Exchange Rate. EViews software is used for the data analysis.

**Key words:** Exchange Rate, ARIMA, ARCH, GARCH, IGARCH, EGARCH, AIC, VAR.

## **CHAPTER 1**

### **INTRODUCTION**

After the conversion of exchange rate from fixed to floating system, exchange rate volatility became an important issue, Exchange rate determines rate of change of currencies, it is a conversion factor (Khan & Azim 2013, Javed & Farooq 2009). Exchange rate volatility is the amount of uncertainty or risk associated with size of changes in the value of currency. A higher volatility means that the value of currency spread out over large range. This means that the price of the currency suddenly change over short period of time in either direction (Mukhtar & Malik, 2010).

Exchange rate is the most important variable for an economy because all countries have its own separate currency and all countries trade internationally, so it's necessary to convert one country's currency in terms of another. Exchange rate is a factor for conversion, it is the value of one country's currency in terms of another country's currency. Exchange rate is the comparison of value of goods and services produced in different countries in an efficient way.

Foreign Exchange rate is necessary for international transaction. It is very important for all countries, it's equally important for emerging as well as for developing countries.

In fact, some professionals have said that exchange rate policies followed by some developing countries after 1970s were inappropriate, and this caused severe overvaluation of their currencies and finally contributed to their debt crises. Such overvaluation may cut exports, harm agriculture and create weakening capital outflows in the developing countries. Problems like energy crisis which became predominant in the 1970s, stimulated a new concern in matters of adjustment and behavior of exchange rate to external shocks since oil was being imported on a large scale by developing as well as emerging.

Before World War II, in the 1930s there was flexible, high volatile exchange rate and competitiveness in exchange rate policies. On 27th December, 1945, the Bretton

Woods conference was held, participants of different countries agreed to begin a period of fixed, but adjustable exchange rate system. It was supposed that a more stable exchange rate system would uphold the development of international trade. It was decided that the parity value of each associate should be expressed in terms of gold as a common denominator or in terms of the US dollar. Moreover, the maximum as well as the minimum rates should not differ from the parity by more than 1%.

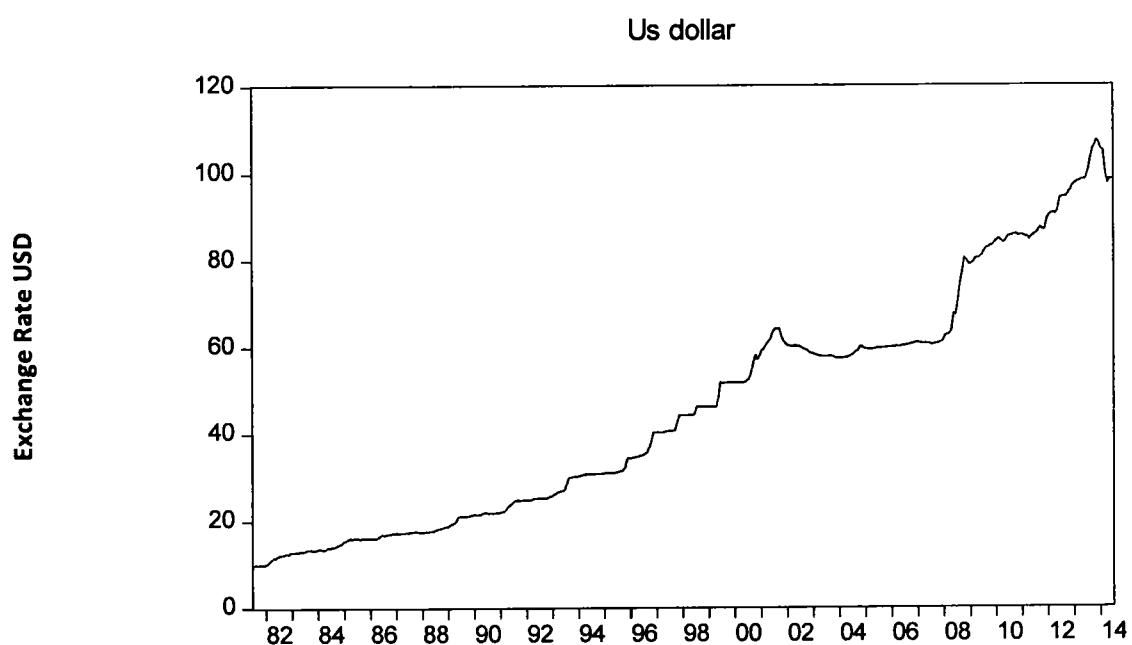
Exchange rate plays an important role in international trade and finance. Exchange rate fluctuations may have significant impact on prices, wages, interest rates, unemployment and level of output (Ramzan, Ramzan & Zahid, 2013). It also influences on decision of policy makers and play an important role to determine the volume of imports and exports. Exchange rate volatility directly influences the prices of exports and imports, manufacturing and their growth rates. Moreover, its effect on allocation of manufacturing goods, reserve money and balance of payments (Javed & Farooq, 2009). It helps to maintain balance of capital in a free market system. The dynamics in exchange rate play an important role to determine trade balance.

The high degree of uncertainty and volatility of exchange fluctuations observed in Pakistan is of great concern to policy-makers and researchers, to investigate the nature and extent of the impact of such fluctuation on Pakistan's volume of trade (Mustafa & Nishat, 2004). In many countries, it is experienced that volatility in exchange rate has reduced the trade by creating about future profit from exports (Mustafa & Nishat, 2004).

Historically, Pakistan's foreign exchange system has remained dynamic under fixed and flexible exchange rate regimes. In the beginning, it was pegged to the Pound Sterling, which continued up to the 1970s in order to keep the exchange rate fixed under the Bretton Woods policy consensus. However, during the early 1970s, the peg-currency (Pound Sterling) was replaced by the US dollar, at PKR 4.76 per USD as an initial exchange rate. The first shock occurred in 1972, when the Rupee fell by 56.7 percent in terms of gold. A flexible currency band accommodating fluctuations up to 4.5 percent was introduced to resolve this issue (Khan & Azim 2013).

Pakistan has tried to incorporate some reforms within the financial sector over time, such as making stock markets accessible to a large number of investors and following a flexible exchange rate policy. Since 1970, the Rupee was depreciated against the US dollar on average from PKR 4.76 to PKR 10.34 in 1970s, to PKR 17.55 in 1980s, to PKR 46.82 during 1990s, and up to PKR 87.16 per US dollar during the 2000s to PKR 98.2 during 2010s (*State Bank of Pakistan*).

**Figure: 1.1** US Dollar Exchange Rate July 1981 to Jun 2014

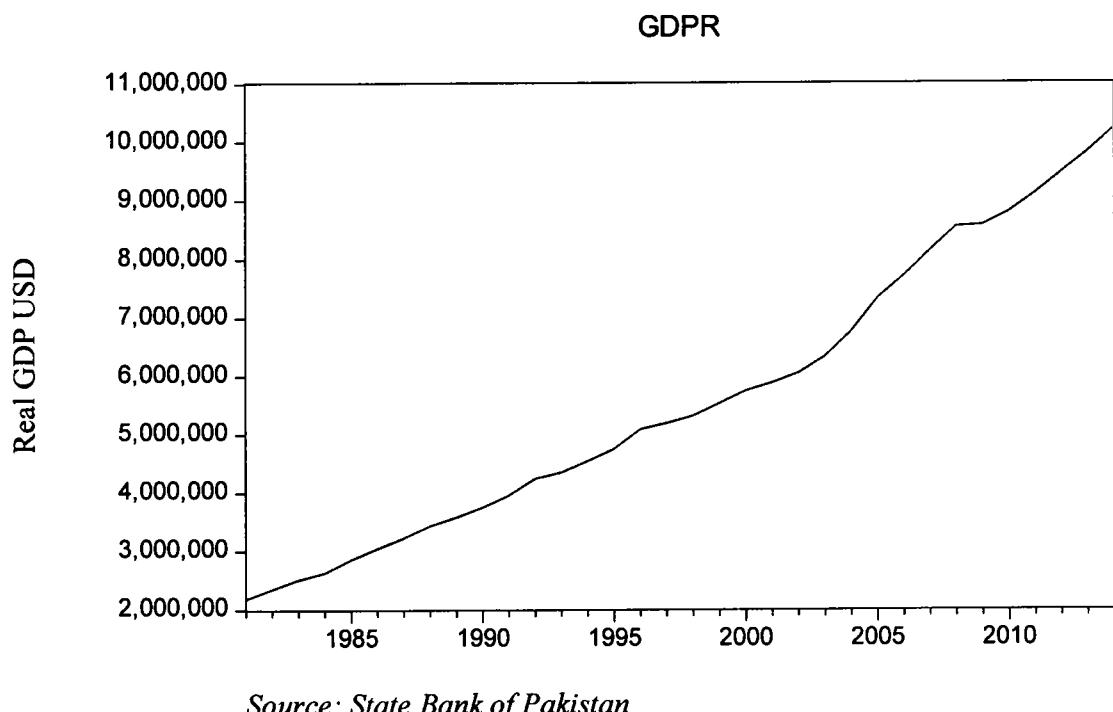


*Source: State Bank of Pakistan*

## 1.1 Real Gross Domestic Product

Gross domestic product (GDP) is the monetary value of all the finished goods and services produced within a country's borders in a specific time period. Gross Domestic Product (GDP) observed during the year 2014 is 243.63 billion USD. GDP in Pakistan averaged 59.54 billion USD. Pakistan's GDP reaching an all-time in the year 2014 and record low of 3.71 billion USD in 1960. (*World Bank Group*).

Figure: 1.2 Real GDP, in US dollar 1981 to 2014

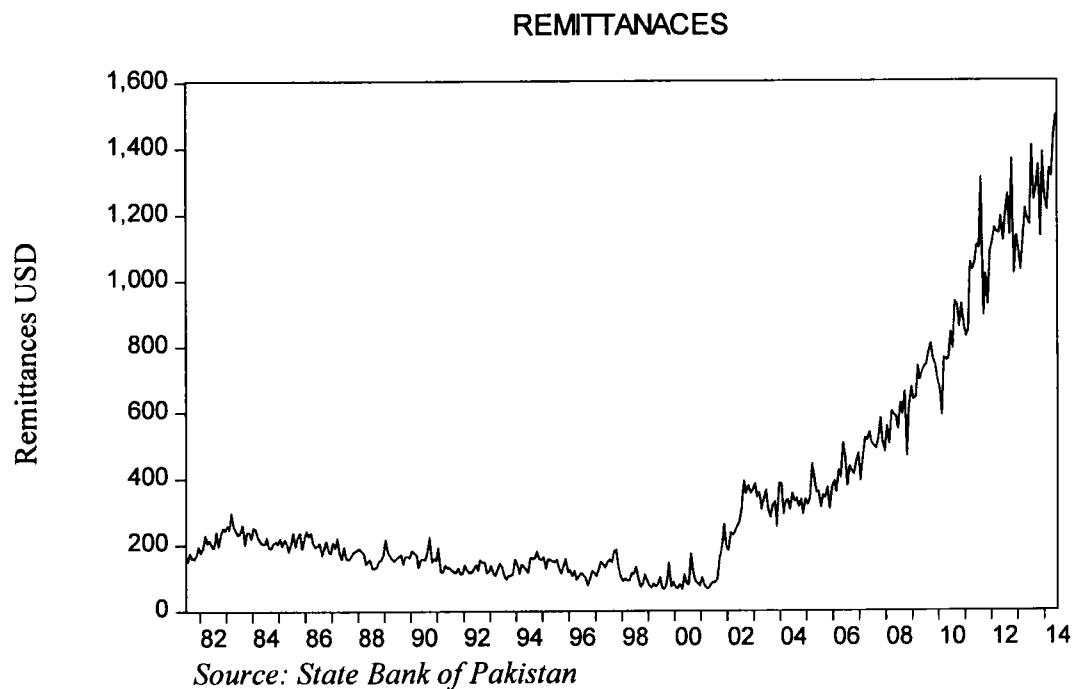


*Source: State Bank of Pakistan*

## 1.2 Foreign Remittances

Worker's remittances are different from FDI, aids and loans it means the transfer of money from migrants to their family in home country. For developing countries like Pakistan it is the largest source of earnings. The foreign exchange in the year 2013-14 the total worker's remittances amount is 15833.67 US million dollars. (*State Bank of Pakistan*).

Figure: 1.3 Foreign Remittance in million USD, July 1981 to June 2014



### 1.3 Inflation Rate

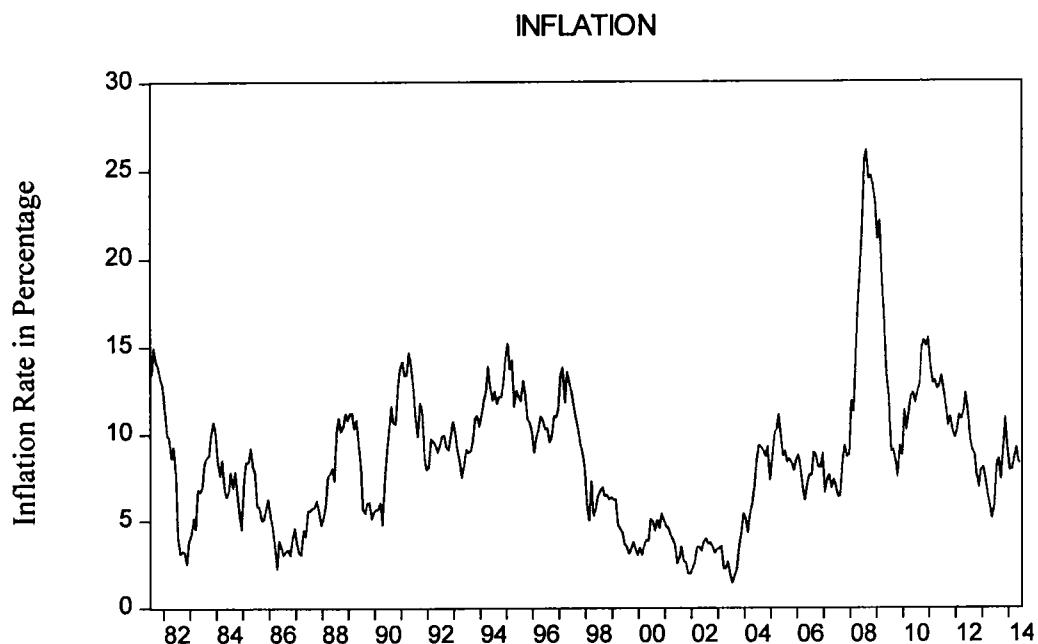
(Fischer, 1993) describes that the relationship between GDP growth Rate and inflation has recognized much attention particularly in the past era. Most empirical results have proven an inverse relationship between GDP growth rate and inflation.

The Relentless rise in prices of goods and services over time, delays efficient Allocation of resource by obscuring the motioning role of relative price variations which is a significant guide for effective decision making.

Inflation makes exports quite expensive, reducing international competitiveness of any country. It makes the cost of living is very high, it has negative effects on balance of payments. It's infect inflation is the public enemy. But in positive sense inflation redistributes real income, encourages employment, increases government revenue and encourages investment.

The inflation rate is recorded during fiscal year 2013-14 is 8.62 from 1981 to 2014 reaching high of 21.03 percent and a recorded low of 3.11 in the year 2002-03. (*State Bank of Pakistan*).

**Figure: 1.4** Inflation Rate July 1981 to June 2014



*Source: State Bank of Pakistan*

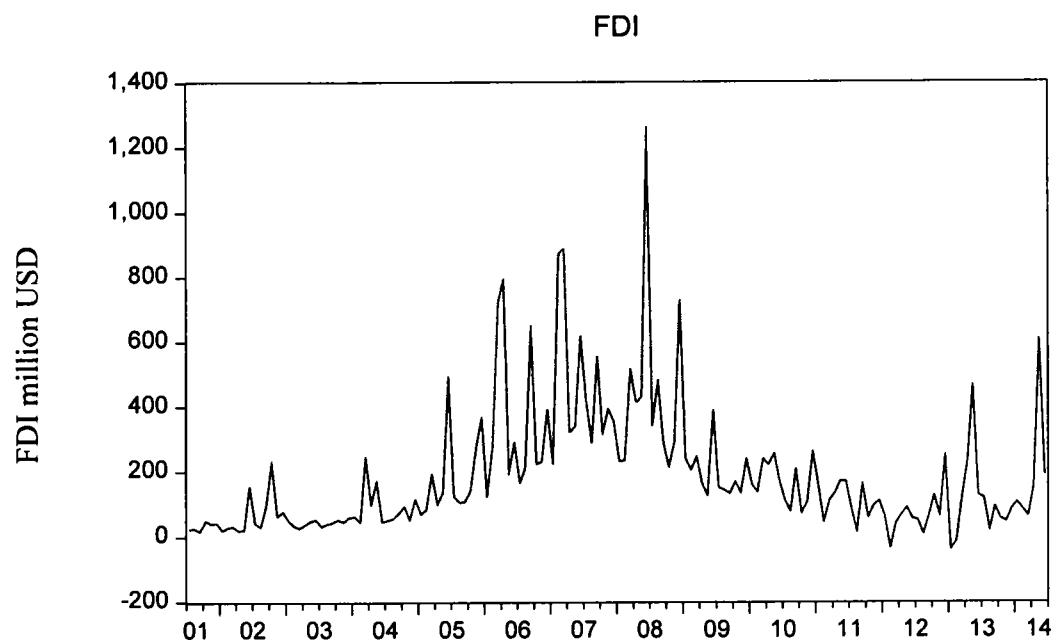
#### **1.4 Foreign Direct Investment (FDI)**

The role of foreign Direct Investment (FDI) for the progress of developing countries is vital. The foreign stakeholders are encouraged to invest in the host country, if the predictions of earning long term revenues by contributing to production sector of that country are very much obvious. FDI not only contributes to capital formation in developing countries, but this investment is also a source of transfer of new technologies and innovative skills from advanced to emerging countries.

In the light of its importance for the progress of developing countries, developing countries offer some incentives to the overseas investors in order to attract Foreign Direct Investment.

Furthermore, these countries take some steps to make certain developments in their environment i.e. law and order situation, security peace in order to make it conducive for investors. Pakistan is facing some serious problems due to law and order situation and political instability. Inflow of Foreign Direct Investment during the fiscal year 2006-07 is 5409.84 million USD which is highest but during the year 2013-14 reached to 1631.26 million USD. Pakistan has been ranked among top ten reforming countries in the world. In terms of ease of doing business Pakistan is at 128th position according to the recent World Bank report. (*World Bank Group, Pakistan Country Partnership Strategy 2015-19*).

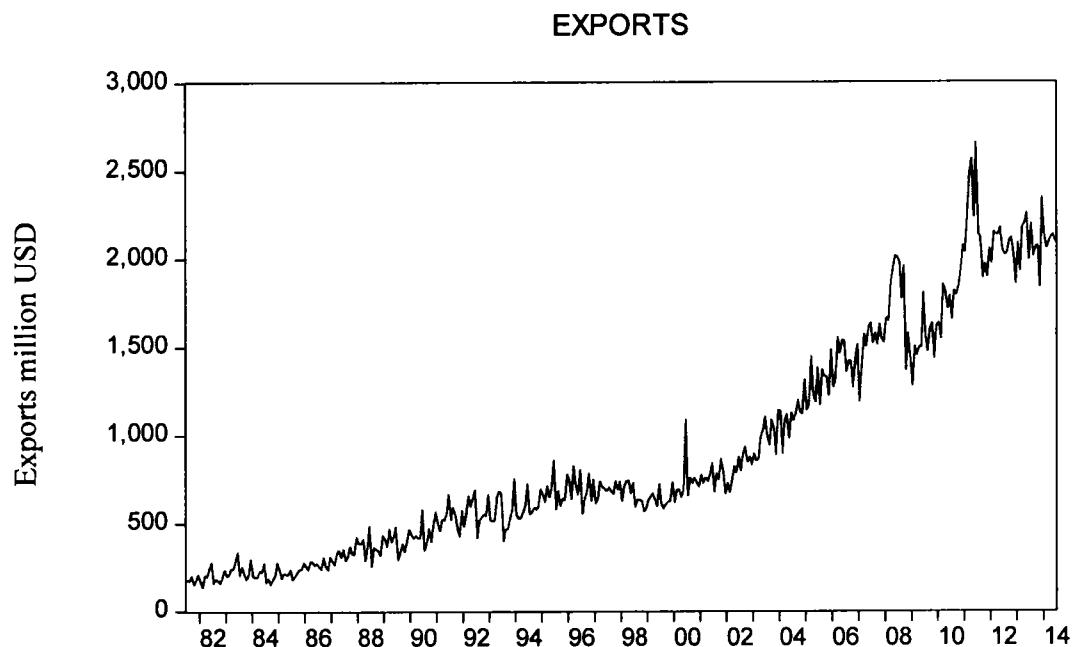
**Figure 1.5 Foreign Direct Investment**



## 1.5 Pakistan's Exports

Exports play a vital role to improve growth of any country. Exports are the source of earnings of a country because it reflected in foreign money. Exports depend on some factors i.e. price of product, economic conditions of importing country and quality of product. Exports have strong effect on exchange rate. During the fiscal year 2010-11 total exports value is 25354.44 million USD which is highest and in last year i.e. 2013-14 is 25162.08 million USD. (*State Bank of Pakistan*).

**Figure : 1.6** Pakistan's Exports in million USD, July 1981 to June 2014



*Source: State Bank of Pakistan*

## **1.6 OBJECTIVES OF THE STUDY**

Followings are the objectives of the study

1. To search the best time series model among ARIMA, ARCH/GARCH family models to capture the exchange rate volatility.
2. To check the significance of ARCH family of model, for modeling and forecasting on Pakistan exchange rate's data.
3. The high degree of volatility and uncertainty of exchange rate fluctuations observed in Pakistan is of great concern to policy makers and researchers to investigate the nature and extent of the impact for such fluctuation on Pakistan's Economy.

## Chapter 2

### REVIEW OF LITRATURE

**According to Engle, (1982) & Bollerslev,(1986)** in financial time series ARCH family of models are more reliable for clustering volatility because these models are specifically designed for volatility modeling.

**Copelman and Werner (1996)**, used VAR model with five variables for Mexico's exchange rate, depreciation of nominal exchange rate, interest rate, and a measure for money balances, revealed that dropped of output are observed after a devaluation.

**Kamin (1996)** indicated that the level of the exchange rate was a main determinant of the inflation rare in Mexico during the period of 1980 and 1990.

**McKenzie, (1999)** investigated that the modeling and forecasting of exchange rate and their volatility has important implications on economics and finance. He compares the ability of ARCH, AR and Mean models to forecast the magnitude of change in 19 Australian bilateral exchange rate series. He has suggested that ARCH model generate superior forecasting performance in situation of squared return of an exchange rate series.

**Kamin and Roger (2000)** observed the influence of depreciation on output and inflation rate of Mexico by applying VAR model with four variables; exchange rate, price index, output, and interest rate of US using quarterly data for the period of 1981-1995.

**AHMAD et al, (2002).** They used GARCH models with modifications for capturing the volatility of the exchange rates. The Q-statistic and LM tests suggest that long memory GARCH models should be used instead of the short-term memory and high order ARCH model. The GARCH models in out-of-sample and one-step-ahead forecasting. When using random walk model as the simple benchmark, all GARCH models outperform this model in forecasting the volatility of the exchange rates.

**Mukherjee et al (2003),** VAR structure is a dominant tool for analyzing impulse responses to systemic shocks and variance decomposing in variables due to these shocks.

**Sandoval (2006)** used the time series models i.e. ARMA, GARCH and EGARCH models for exchange rate modeling and capturing significant characteristic of data. He took four years daily exchange rate data from 2000 to 2004 from Asian and Latin American countries.

**Suliman Zakaria Suliman Abdalla, (2012)** used the generalized autoregressive conditional heteroscedastic approach to model the exchange rate volatility of nineteen Arab countries using daily returns over the period of 1st January 2000 to 19th November 2011. He applies both symmetric and asymmetric models that capture most common stylized facts about exchange rate returns such as volatility clustering and leverage effect. Based on the GARCH (1,1) model. Moreover, the asymmetrical EGARCH (1,1) results provide evidence of leverage effect for majority of currencies, indicating that negative shocks imply a higher next period volatility than positive shocks. Finally, the paper concludes that the exchange rates volatility can be adequately modeled by the class of GARCH models.

**Abdullah, (2012)** applied time series modeling for estimation and forecasting of gold bullion prices. He has concluded that ARIMA (2, 1, 2) is best model to forecast the price of gold bullion.

**Asad, (2012)** predicted the electricity demand in Australia for first seven days of May, 2011. He has used one year data of fiscal year 2010 to 2011. He has selected the ARIMA model for forecasting electricity demand and used Root Mean Square Error (RMSE) and Mean Absolute Percentage Error (MAPE) to measure the accuracy of forecast.

**Ramzan et al. (2012)** explained that ARCH families of model are best for prediction of exchange rate. They also studied the working of GARCH model, and concluded that GARCH (1,2) is best model for removing persistence in volatility. Moreover, EGARCH (1,1) successfully overcome the leverage effect in the exchange rate returns. They also investigated the performance of GARCH family models in forecasting the volatility behavior of Pakistan foreign exchange market, and found that the EGARCH based evaluation of foreign exchange rates showed asymmetric behavior of volatility, where TARCH model showed insignificant.

**Muhsin et al (2012).** Examined the performance of GARCH family models including EGARCH model in forecasting the volatility behavior of Pakistan's Exchange market. Daily Exchange rates data, from January, 2001 to December, 2009 was used for volatility capturing.

**Corliss, (2013)** shows that ARIMA is the most suitable for modeling and forecasting financial data. He reviewed the basic statistical concepts of ARIMA model and its application in statistical research.

**Devi et al, (2013)** they have selected top 4 companies from the Nifty Midcap50. Time series data of 5 years has selected and applied ARIMA model for forecasting. To check the accuracy of model they applied Akaike info Criterion and Bayesian info Criterion.

**Obeng et al. (2013)**, they have proved in their study that the relationship between exchange rate and GDP growth rate is positive, to check the correlation between both variable they used Pearson's Product Moment Correlation Coefficient (PPMC).

**Steve c, (2014)** analyzed exchange rate data of Naira/Dollar through ARIMA model. He has used 29 years data from 1982 to 2011 and concluded that the ARIMA model is most suitable for modeling and forecasting of exchange rate of Naira/Dollar.

## CHAPTER 3

### RESEARCH METHODOLOGY

#### 3.1. Source of Data

For volatility modeling and forecasting, the data used in present study consist average foreign exchange rates of Pakistan (Pak rupees per US \$). Monthly and yearly exchange rate data from 1981 to 2014, obtained from State Bank of Pakistan (SBP). Different time series model are used to model this data like ARMA, ARIMA ARCH and GARCH family of models. To investigate the effect of Exchange Rate's volatility on the Real Gross Domestic Product (GDP) of Pakistan. The study has used six variables, the data for the variables i.e. Inflation Rate (INF), Foreign Direct Investment (FDI), Exports, Real GDP and Foreign Remittances obtained from The State Bank of Pakistan. employing The empirical relationship between exchange rate volatility and Real Gross Domestic Product (GDP) have been found while employing an econometric study based on Vector Autoregressive (VAR) methodology for yearly data collected from 1981 to 2014..

#### 3.2. Time Series Models

##### 3.2-1 Time Series

CHATFIELD (2001) defines that “A time series is a set of observations measured sequentially through time”.

##### 3.2-2 Univariate Time Series

The term univariate means a time-series that consist only one variable recorded chronologically through time in this study i.e. Exchange rate.

##### 3.2-3 Time Series Model

Time series model based on mathematical representations and theoretical foundations. An econometric model has to fulfil the following qualities, FROHN (1995)

- theoretical plausibility

- reliable parameter estimation
- good adjustment (i.e. the process that generates the data should be captured)
- good forecast
- simplicity (i.e. a model with less variables or easier functional form should be preferred)

### **3.2-4 ACF (Autocorrelation Function)**

The important properties of any random variable are the first, two moments, i.e. its mean and the variance. The time series is the stochastic process. The relationship between different time periods is very important.

This is known as autocorrelation or we can say that auto-covariance. The auto-covariance function ( $X_k$ ) of a time-series is defined as:

$$\gamma_k = E \{ [X_t - E(X_t)][X_{t-k} - E(X_{t-k})] \},$$

Where,  $Y_t$  stands for the time-series. The autocorrelation function ( $\rho_k$ ) is defined as:

$$\rho_k = \frac{\gamma_k}{\gamma_0}$$

and the graph of this function is called correlogram. The correlogram is very important for the analysis, because it contained observed series which is time dependent. Since  $X_k$  and  $\rho_k$  only differ in the constant factor  $X_0$ , i.e. the auto variance of the time-series, it is sufficient to plot just one of these two functions.

Correlogram is used for inspection the randomness in the data. If these autocorrelations are close to zero for any or all time lags then the data is random. It also used to identify the order of an AR and MA process.

On the vertical axis the autocorrelation coefficients ( $X_k$ ) and on the horizontal axis the time lag.

### 3.2-5 PACF (Partial Autocorrelation Function)

The PACF ( $\pi_k$ ), where  $k \geq 2$ , is defined as the partial correlation between  $Y_t$  and  $Y_{t-k}$  under farm the random variables between  $Y_u$ . It looks to be clear, that the PACF is defined for lags equal to two or greater. The partial correlogram is also used for model identification in Box & Jenkins models. On the y-axis they display the partial autocorrelations coefficients and on the x-axis the time lag  $k$ .

### 3.2-6 Augmented Dickey-Fuller Test

In case of time series analysis stationary of the data is very important otherwise classical linear regression model (CLRM) assumption will be not valid and estimates of parameters will not be Best Linear Unbiased (BLUE) estimators and results may be spurious. To check the stationary of time series data the Augmented Dickey-Fuller unit root test is best. Stationary can be confirmed through first order difference or higher orders difference of the series. Augmented Dickey-Fuller (ADF) has following structure.

$$EX_t = \alpha + \beta_t + \gamma EX_{t-1} + \sum_{k=1}^p \delta_k \Delta EX_{t-k} + e_t$$

Where EX (Exchange Rate) is the variable under consideration,  $\Delta$  is first difference operator,  $t$  captures any time trend,  $e_t$  is a random error  $p$  is the maximum lag length while  $\alpha, \beta, \gamma$  and  $\delta$  are the parameters be estimated.

### 3.2-7 ARMA (Autoregressive and Moving Average) Models

The ARMA model is the combination of an autoregressive (AR) and Moving Average (MA) Models. In an ARMA (p,q) process there are two integers (p,q) where p is autoregressive and q is moving average.

$$EX_t = \varphi_0 + \varepsilon_t + \sum_{i=1}^p \varphi_i EX_{t-i} + \sum_{i=1}^q \theta_i \varepsilon_{t-i}$$

Where

$\phi_1, \phi_2, \dots, \phi_p$  Are the coefficients of auto-regressive.

$\theta_1, \theta_2, \dots, \theta_p$  Are the coefficients of moving averages.

For the stationary process it must have constant Mean  $u$  for all time periods. It is assumed that the mean of  $y_t$  and  $\varepsilon_t$  are uncorrelated random variables with

$$E[\varepsilon_t] = 0 \text{ and } \text{var}[\varepsilon_t] = \sigma_t^2.$$

### 3.2-8 ARIMA (Autoregressive Integrated Moving Average) Models

The model is developed by Box & Jenkins (1976), we shall use this model for exchange rate volatility forecasting. Model is a combination of autoregressive (AR) and moving average (MA). An ARIMA (p, d, and q) is

$$\phi(L)(1 - L)^d EX_t = \theta_q(L)\varepsilon_t$$

$$(1 - \phi_1 L - \phi_2 L - \dots - \phi_p L^p)EX_t = (1 - \theta_1 L - \theta_2 L^2 - \dots - \theta_q L^q)\varepsilon_t$$

Where,  $EX_t$ , represent the exchange rate, L is the lag operator.

$\phi_1, \phi_2, \dots, \phi_p$  are autoregressive parameters

$\theta_1, \theta_2, \dots, \theta_p$ , are moving average parameters

$\varepsilon_t$  is error term,

p, d and q denote the autoregressive, differenced order and moving average parameters.

### 3.2-9 ARCH (Autoregressive Conditional Heteroscedasticity) Model

It is a nonlinear model which is specifically built for volatility capturing. It has wide application in finance. It is an extension of AR (Autoregressive) model and its various extension from ARMA(p,q) model, we assume that error terms is white noise, stochastic process i.e.  $\mu_i \sim N(0, \sigma^2)$ . However, it is unlikely in the context of same time series,

especially financial time series that the variance of the error will be constant over time i.e. Heteroscedasticity. Another important feature is that volatility clustering exist in financial time series which leads us to construct such a model that would be able to capture the phenomena of volatility clustering of the time series by allowing to vary the variance of residual in the model i.e.

If the model is AR (1)

$$EX_t = \varphi_0 + \varphi_1 EX_{t-1} + \epsilon_t$$

And ARCH (1) model is

$$\sigma_t^2 = \alpha_0 + \alpha_1 \epsilon_{t-1}^2$$

$\sigma_t^2$  Depends on lag square term  $\epsilon_{t-1}^2$ .

It is assume that in ARCH models, variance of the current error term is related to the size of the previous time periods, error term, often the variance is related to square of the previous innovations. Engle, (1982) introduced ARCH model, these models apply on modelling financial time series that exhibit time varying clustering.

Let  $\epsilon_t$  denotes error terms, and  $\epsilon_t$  are split into two pieces  $z_t$  stochastic and  $\sigma_t$  time dependent standard deviation, so that

$$\epsilon_t = \sigma_t z_t$$

Where  $z_t \sim iid N(0,1)$  and the series  $\sigma_t^2$  are modeled by

$$\sigma_t^2 = \alpha_0 + \sum_{i=1}^q \alpha_i \epsilon_{t-i}^2$$

Where  $\alpha_0 > 0$  and  $\alpha_i \geq 0, i > 0$

### 3.2-10 GARCH (Generalized Autoregressive Integrated Moving Average) Model

There is some limitations of ARCH (q) model which first the decision of the value of “q” is difficult task and second is the value of “q” to capture all of the dependence in the conditional variance might be large, resultantly, a large conditional variance of the

model. Due to the above limitations ARCH (q) model has been extended to GARCH model which overcomes some of the problems of ARCH (q) model. The GARCH models were developed by Engle, (1982) & Baillie, (1986), GARCH family model have proved successful in forecasting volatility in many situation. It allows the conditional variance to be dependent upon previous own lags along with lag residual terms i.e. The GARCH (p,q) model is formulated as

$$\begin{aligned}\sigma_t^2 &= \alpha_0 + \alpha_1 \varepsilon_{t-1}^2 + \cdots + \alpha_q \varepsilon_{t-q}^2 + \beta_1 \sigma_{t-1}^2 + \cdots + \beta_p \sigma_{t-p}^2 \\ &= \alpha_0 + \sum_{i=1}^q \alpha_i \varepsilon_{t-i}^2 + \sum_{i=1}^p \beta_i \sigma_{t-i}^2\end{aligned}$$

Where q is the order of the ARCH terms, and p is the order of the GARCH terms.

$\sigma_t^2$  may be interpreted as a weighted function of a long term average value that gives us long term average value that gives us information about volatility during the previous period ( $\alpha_1 \varepsilon_{t-1}^2$ ) and the fitted variance from the model during the previous period ( $\beta_1 \sigma_{t-1}^2$ ).

### **3.2-11 IGARCH (Integrated Generalized Autoregressive Integrated Moving Average) Model**

GARCH models apply both autoregressive and moving average structure to the variance,  $\sigma_t^2$ . The IGARCH is specified as

$$\varepsilon_t = \sigma_t z_t; \sigma_t^2 = \alpha_0 + \sum_{i=1}^q \alpha_i \varepsilon_{t-i}^2 + \sum_{j=1}^p \beta_j \ln \sigma_{t-j}^2$$

Integrated Generalized Autoregressive Conditional Heteroscedasticity (IGARCH) is a restricted version of the GARCH model, where the sum of persistence parameters sum up to 1, and therefore there is a unit root in the GARCH process. The condition for this is:

$$\sum_{i=1}^p \beta_i + \sum_{i=1}^q \alpha_i = 1$$

However if sum of  $\alpha$ 's and  $\beta$ 's is one or more, then there will be problem of unit root in the autoregressive representation for squared returns. To account for this problem integrated GARCH is used.

### 3.2-12 EGARCH (Exponential Generalized Autoregressive Integrated Moving Average) Model

The Exponential General Autoregressive Conditional Heteroscedasticity model is a popular GARCH model which is developed by Nelson (1991). EGARCH model is successfully capture the leverage effect and ensures that the variance is always positive even if the parameters may be negative.

The EGARCH is generally specified as

$$\varepsilon_t = \sigma_t z_t; \ln \sigma_t^2 = \alpha_0 + \sum_{i=1}^q \alpha_i \varepsilon_{t-i}^2 + \sum_{j=1}^p \beta_j \ln \sigma_{t-j}^2$$

The following model also used in the financial data, (Dhamija and Bhalla)

$$\ln \sigma_t^2 = \alpha + \beta_i \varepsilon_{t-1}^2 + \sum_{j=1}^p \gamma_j \ln(\sigma_{t-j}^2) + \sum_{i=1}^p \omega_i \left( \frac{|\varepsilon_{t-1}|}{\sigma_{t-1}} \sqrt{\frac{2}{\pi}} \right)$$

### 3.3 Comparison Methods

For the purpose of comparison of forecasting performance the Mean Absolute Error, Mean Absolute Percentage and Root Mean Square Error and Theil's inequality coefficient U are commonly used. These measures use for evaluation of forecasting performance.

### 3.3-1 Mean Absolute Error

The Mean absolute error (MAE) is the common measure of forecast error in time series analysis. It is dependent on the scale of the dependent variable. It is less sensitive than the usual loss to large deviation.

$$MAE = \frac{1}{n} \sum_{i=1}^n |\hat{EX}_t - EX_t|$$

### 3.3-2 Mean Absolute Percentage Error

The Mean absolute percentage error (MAPE) is scale independent accuracy measure. It is also referred as Mean absolute percentage deviation (MAPD). There are some important problems MAPE is affected are: (1) Absolute percentage error is greater if equal errors above the actual value; (2) When the value of the original series is small then percentage errors will be large; (3) while in empirical studies outliers may distort the comparison

$$MAPE = \left[ \frac{1}{n} \sum_{i=1}^n \left| \frac{(\hat{EX}_t - EX_t)}{EX_t} \right| \right] \times 100$$

### 3.3-3 Root Mean Square Error

The Root mean square error (RMSE) is frequently used accuracy measure. It is depend on the scale of the dependent variable. It is relative measure to compare forecasts for the same series across different models. Problem with RMSE forecast error variance vary across time because of variation in exogenous variables and nonlinearities in the model.

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (\hat{EX}_t - EX_t)^2}$$

### 3.3-4 Theil's Inequality Coefficient

The Theil inequality coefficient is scale invariant and it always lies between 0 and 1, where 0 indicates perfect fit.

$$U = \frac{\sqrt{\frac{1}{n} \sum_{t=1}^n (\widehat{EX}_t - EX_t)^2}}{\sqrt{\frac{1}{n} \sum_{t=1}^n \widehat{EX}_t^2} + \sqrt{\frac{1}{n} \sum_{t=1}^n EX_t^2}}$$

## 3.4 Vector Autoregressive (VAR) MODEL:

The general VAR model for this study is specified as

VAR structural Model

$$BY_t = r_1 Y_{t-1} + \dots + r_p Y_{t-p} + \varepsilon_t$$

VAR Model reduced form is

$$Y_t = \gamma_1 Y_{t-1} + \dots + \gamma_p Y_{t-p} + e_t$$

Where  $Y_t = (6 \times 1)$  vector of system endogenous variables at time t such as Exchange Rate, Gross Domestic Production (GDP), Exports, Foreign Direct Investment (FDI), Inflation Rate and Foreign Remittances.

$Y_{t-1}$  are lagged values of the system endogenous variables,  $t = 1, 2, \dots, p$

$\gamma_i = (6 \times 6)$  matrices of determined variables coefficient to be estimated,  $i = 1, 2, \dots, p$

$e_t = (6 \times 1)$  vector of innovations at time t .

### 3.4-1 Impulse Response Function (IRF)

**Objective:** the reaction of the system to a shock

$$Y_t = \gamma_1 Y_{t-1} + \cdots + \gamma_p Y_{t-p} + e_t$$

The term  $e_t$  represents innovations in the system.

If the system is stable,

$$Y_t = \mu + \emptyset(L)e_t = \mu + e_t + \emptyset_1 e_{t-1} + \emptyset_2 e_{t-2} + \cdots$$

$$\emptyset(L) = [\gamma(L)]^{-1}$$

Redating at time  $t+s$

$$Y_{t+s} = \mu + e_{t+s} + \emptyset_1 e_{t+s-1} + \emptyset_2 e_{t+s-2} + \cdots + \emptyset_s e_t + \emptyset_{s+1} e_{t-1} + \cdots$$

$$\frac{\partial Y_{t+s}}{\partial e_t} = \emptyset_s = [\emptyset_{ij}^{(s)}] \quad S \text{ is a multiplier}$$

$$\frac{\partial Y_{i,t+s}}{\partial e_{jt}} = [\emptyset_{ij}^{(s)}] \quad \text{Reaction of the } i \text{ variables to a unit change in innovation } j$$

The interpretation of the  $\emptyset$  matrices is that they symbolizes marginal effects, or the model's reaction to a unit innovation at time  $S$  in every of the variable

### 3.4-2 Impulse Response Function

Response of  $Y_{i,t+s}$  to one-time impulse in  $Y_{jt}$  with all other variables time  $t$  or earlier is constant. Normally an impulse response function traces the influence of a one-time shock to one of the innovations on present and future values of the endogenous variables

$$\frac{\partial Y_{i,t+s}}{\partial e_{jt}} = \emptyset_{ij}^s$$

## Chapter 4

### RESULTS AND DISCUSSIONS

#### 4.1 The Augmented Dickey–Fuller (ADF) test

The Augmented Dickey–Fuller (ADF) test is presented in table 4.1. The result shows that all the variables are not stationary at level and stationary at first difference. It is essential to check the stationarity of the data before using the time series models like Autoregressive Moving Average (ARMA), Autoregressive Integrated Moving Average (ARIMA), Autoregressive Conditional Heteroscedasticity (ARCH), Generalized Autoregressive Conditional Heteroscedasticity (GARCH), Integrated Generalized Autoregressive Conditional Heteroscedasticity (IGARCH) and Exponential General Autoregressive Conditional Heteroskedastic (EGARCH), which are being used in this study.

**Table: 4.1** Unit Root test

Variable	Level		First Difference	
	Constant	Constant and Trend	Constant	Constant and Trend
GDP	-0.57	-1.91	-5.10**	-5.03**
Export	-1.85	-1.52	-6.28***	-6.58**
Yearly Exchange rate	-0.15	-1.77	-4.45***	-3.87**
FDI	-2.30	2.56	-4.90**	-4.92***
Inflation rate	-2.59	-2.55	-6.59**	-6.50***
Remittances	-0.93	-1.33	-5.09**	-5.07**
Monthly Exchange Rate	0.7954	-1.9566	-12.4775***	-12.5518***

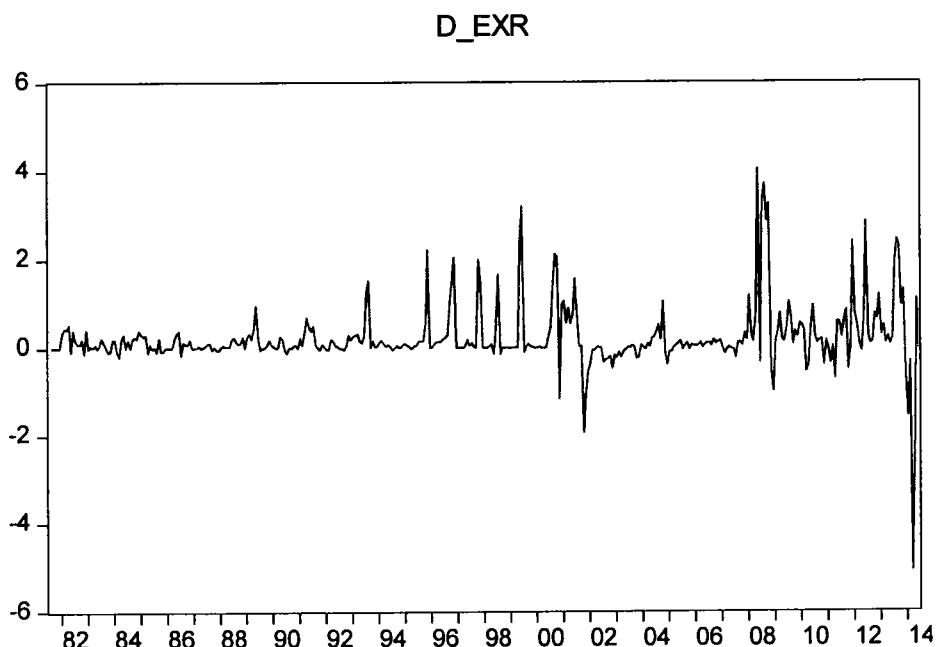
\*\*\* Significant at 1% level

\*\* Significant at 5% level

The above table 4.1 shows the stationary level of exchange rate. Results indicate that exchange rate is integrated of level one. It is stationary at first difference. The correlogram and graphical representation of Exchange Rate shows in Figure 4.1 and Table 4.2 no trend in data hence, suggesting that the exchange rate data is stationary.

Figure: 4.1. Representation of Exchange Rate stationary at first difference

Graph: 4.1 Graphical representation of Exchange Rate at first difference



**Table 4.2. Auto Correlation and Partial Auto Correlation of Exchange Rate**

No	AC	PAC	Q-Stat	Prob
1	0.431	0.431	73.943	0.000
2	0.204	0.022	90.564	0.000
3	0.163	0.083	101.19	0.000
4	0.010	-0.114	101.23	0.000
5	0.018	0.049	101.37	0.000
6	-0.006	-0.036	101.38	0.000
7	-0.101	-0.094	105.49	0.000
8	-0.039	0.041	106.12	0.000
9	0.044	0.084	106.92	0.000
10	0.053	0.031	108.07	0.000

After taking the first difference of the exchange rate data and transformed sample Autocorrelation function (ACF) and Partial Autocorrelation Function (PACF) shows that the exchange rate series is now become stationary.

#### 4.2 Model Fitting

Model fitting is well-known as model identification, generally starts with autocorrelation analysis. We can draw the conclusion about a suitable model through the time series plot and correlogram. Now for checking the autoregressive pattern the below table 4.4 shows the Autoregressive process of difference Exchange rate returns.

**Table 4.3** Autoregressive model Variable Difference of Exchange Rate

Model	Coefficients									
	ar (1)	ar (2)	ar (3)	ar (4)	ar (5)	ar (6)	ar (7)	ar (8)	ar (9)	ar (10)
AR(1)	.43***	-	-	-	-	-	-	-	-	-
AR(2)	.42***	.02	-	-	-	-	-	-	-	-
AR(3)	.42*	-.02	.09*	-	-	-	-	-	-	-
AR(4)	.43***	-.01	.14**	-.13**	-	-	-	-	-	-
AR(5)	.43***	-.02	.13**	-.15**	.05	-	-	-	-	-
AR(6)	.44***	-.02	.14**	.15**	.07	-.04	-	-	-	-
AR(7)	.43***	-.02	.12**	-.14**	.07	.02	-.13**	-	-	-
AR(8)	.44***	-.02	.12**	-.13**	.06	.02	-.15**	.06	-	-
AR(9)	.43***	-.00	.12**	-.14**	.07	.01	-.15**	.01	.11*	
AR(10)	.43***	-.00	.13**	-.14**	.07	.01	-.15**	.01	.09	.04

\*\*\* Significant at 1% level of Significance

\*\* Significant at 5% level of Significance

Above table 4.3 shows models of Autoregressive process in rows with capital letter while their coefficients are shown in columns with small alphabets. It is clear that the coefficients are significant up to AR (9). We can conclude that Exchange Rate is an AR (9) Process. Smallest Akaike info criterion (AIC) value 1.9697 shows AR (1) is better fitted model amongst Autoregressive AR models.

**Table: 4.4. Moving Average model Variable Difference of Exchange Rate**

Model	Coefficients									
	ma (1)	ma (2)	ma (3)	ma (4)	ma (5)	ma (6)	ma (7)	ma (8)	ma (9)	ma (10)
MA(1)	.41 ***	-	-	-	-	-	-	-	-	-
MA(2)	.42 ***	.08	-	-	-	-	-	-	-	-
MA(3)	.24 ***	.17** *	.18** *	-	-	-	-	-	-	-
MA(4)	.43 ***	.17** *	.17** *	-.01	-	-	-	-	-	-
MA(5)	.43 ***	.17** *	.18** *	-.002	.02	-	-	-	-	-
MA(6)	.44 ***	.19** *	.20** *	.02	.06	.09	-	-	-	-

\*\*\* Significant at 1% level of Significance

\*\* Significant at 5% level of Significance

Above table 4.4 shows models of Moving Average (MA) in rows with capital letter while their coefficients are shown in columns with small alphabets. It is clear that the coefficients are significant up to MA (3). We can conclude that Moving Average is an MA (3) Process. Smallest Akaike info criterion (AIC) value 1.9583 shows MA (3) is better fitted model amongst Autoregressive MA models.

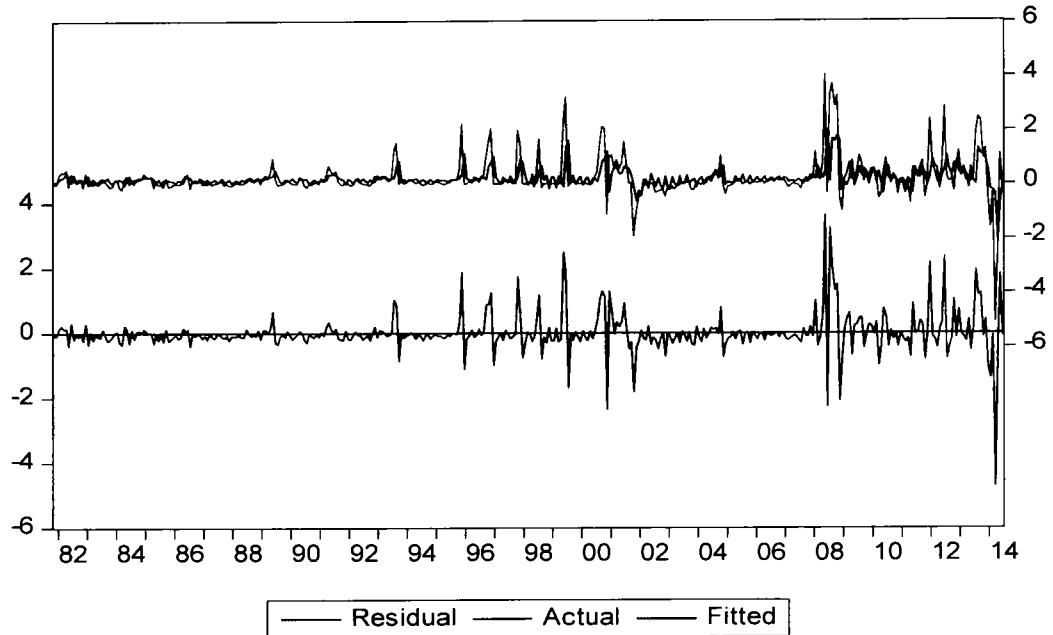
**Table: 4.5. Autoregressive Integrated Moving Average (ARIMA)**

ARIMA	SIC	AIC	LM
1 1 1	2.004	1.9740	Reject $H_0$
1 1 2	2.0160	1.9756	Accept $H_0$
1 1 3	2.0163	1.9658	Reject $H_0$
2 1 1	2.0167	1.9762	Accept $H_0$
2 1 2	2.0239	1.9733	Accept $H_0$
2 1 3	2.0142	1.9536	Accept $H_0$
3 1 1	2.0226	1.9720	Accept $H_0$
3 1 2	2.0124	1.9516	Accept $H_0$
3 1 3	2.0264	1.9554	Accept $H_0$
4 1 1	2.0350	1.9741	Reject $H_0$
4 1 2	2.0292	1.9582	Accept $H_0$
4 1 3	2.0376	1.9564	Accept $H_0$
5 1 1	2.0524	1.9812	Accept $H_0$
5 1 2	2.0441	1.9627	Accept $H_0$
5 1 3	2.0160	1.9244	Reject $H_0$
6 1 1	2.0670	1.9855	Reject $H_0$
6 1 2	2.0349	1.9432	Accept $H_0$
6 1 3	2.0635	1.9616	Accept $H_0$
7 1 1	2.0736	1.9817	Accept $H_0$
7 1 2	2.0852	1.9831	Accept $H_0$
7 1 3	2.0624	1.9501	Accept $H_0$
8 1 1	2.0821	1.9798	Accept $H_0$
8 1 2	2.0913	1.9788	Accept $H_0$
8 1 3	2.0962	1.9734	Accept $H_0$

Accept  $H_0$  means there is no serial correlation

Table 4.5 shows the different combination of ARIMA models for checking the serial correlation we performed LM test. For selection of best model amongst ARIMA models we used AIC and SIC criterions and we conclude that the ARIMA (3,1,2) is best fitted model amongst ARIMA models.

**Graph: 4.2 Actual, Fitted, Residual Graph**



Residual of low volatility tends to be followed by periods of low volatility for a prolonged periods and periods of high volatility is followed by periods of high volatility for a prolonged periods when this thing is happen for residual then we have the justification to run ARCH family of model

**Table: 4.6 ARIMA (3,1,2) model, Monthly Exchange Rate**

Variable	Coefficient	Standard Error	t-statistic	p-value
Constant	0.227279	0.060337	3.766837**	0.0002
AR(1)	-0.639882	0.051818	-12.34872**	0.0000
AR(2)	-0.454253	0.057560	-7.891750**	0.0000
AR(3)	0.482224	0.046453	10.38089**	0.0000
MA(1)	1.077240	0.033861	31.81365**	0.0000
MA(2)	0.944986	0.033872	27.89856**	0.0000

Note: \*\* show significant at 1%

$$EX_t = 0.2272 + 0.63988 EX_{t-1} + 0.4525 EX_{t-2} + 0.4822 EX_{t-3} + 1.0772 \epsilon_{t-1} + 0.9449 \epsilon_{t-2}$$

Table 4.6 shows the variable of ARIMA (3, 1, 2) model on the basis of correspondence p-values we can conclude that all the variable are highly significant.

**Table: 4.7 The LM test on ARIMA(3,1,2)**

Adj R-squared	DW Stat	F-stat	LM-test F-stat	LM-test P-value
0.210254	1.985371	21.81916	0.6884	0.6833

ARCH effect even at 1% level of significance.

#### 4.5 ARCH Test on ARIMA (3,1,2)

The Autoregressive Conditional Heteroscedasticity (ARCH) family of models necessitates the existence of 'ARCH effect' in the residuals. For testing the presence of ARCH effect, use the Lagrange Multiplier (LM) test for differential exchange rate returns series. The results of LM test are presented in Table 4.7. The *p*-value shows that there is indication of ARCH effect. Hence, we reject the null hypothesis of nonappearance of ARCH effect.

**Table: 4.8 ARCH-LM test on ARIMA (3,1,2)**

Lag(P)	Obs-R <sup>2</sup>	Df	Prob.> Chi <sup>2</sup>
1	17.58337	1	0.0000

$H_0$ : There is no ARCH effect and alternate is  $H_1$ : there is ARCH (p) disturbance

The above Table 4.8 shows that the ARIMA (3,1,2) model has ARCH effect, hence we have the evidence to perform the ARCH family of model for capturing the volatility of exchange rate returns.

**Table: 4.9 ARIMA (1,1,2) Model, Yearly Exchange Rate**

Variable	Coefficient	Standard Error	t-statistic	p-value
C	0.614708	0.677443	0.907395	0.0319
AR(1)	0.755466	0.153229	4.930294	0.0000
MA(1)	-0.790940	0.262502	-3.013078	0.0054
MA(2)	-0.933684	0.264170	-3.534402	0.0014

Note: \*\* show significant at 1%

$$EX_t = 0.614708 + 0.755466EX_{t-1} - 0.790940 \epsilon_{t-1} - 0.933684\epsilon_{t-2}$$

Table 4.9 shows the variable of ARIMA (1, 1, 2) model on the basis of correspondence p-values we can conclude that all the variable are highly significant.

**Table: 4.10 The LM test on ARIMA(1,1,2)**

Adj-R-squared	DW-Stat	F-stat	LM-test F-stat	LM-test P-value
0.189405	1.969754	5.14016	0.117334	0.8897

ARCH effect even at 1% level of significance.

#### 4.5-1 ARCH Test on ARIMA (1,1,2)

The Autoregressive Conditional Heteroscedasticity (ARCH) family of models necessitates the existence of 'ARCH effect' in the residuals. For testing the presence of ARCH effect, use the Lagrange Multiplier (LM) test for differential exchange rate returns series. The results of LM test are presented in Table 4.10. The *p*-value shows that there is indication of ARCH effect. Hence, we reject the null hypothesis of nonappearance of ARCH effect.

**Table: 4.11 ARCH-LM test on ARIMA (1,1,2)**

Lag(p)	Obs-R <sup>2</sup>	Chi <sup>2</sup>	Prob. > Chi <sup>2</sup>
1	0.254045	1	0.0000

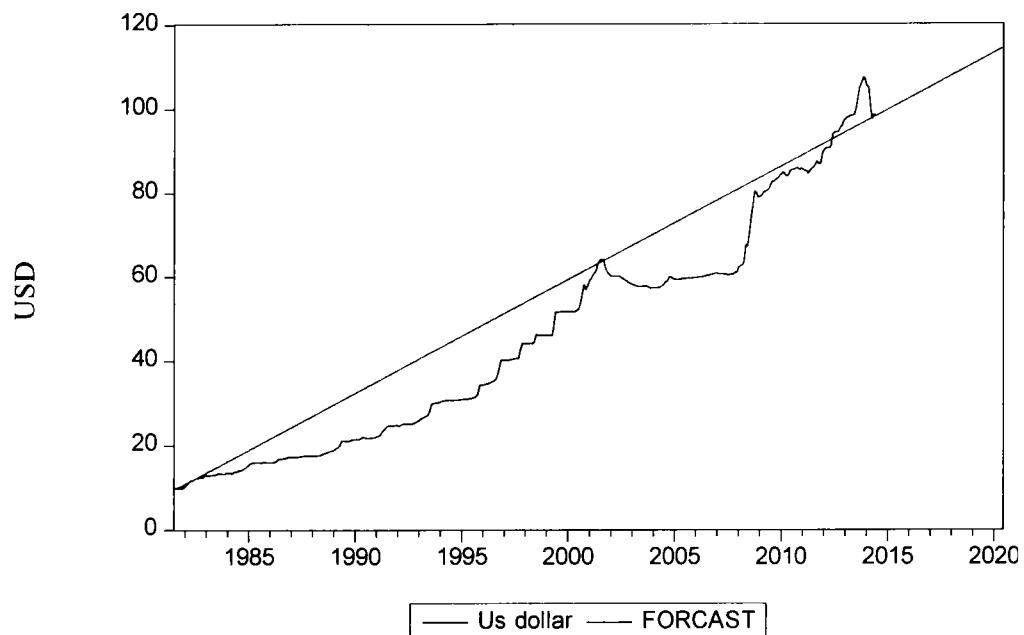
$H_0$ : There is no ARCH effect and alternate is  $H_1$ : there is ARCH (p) disturbance

The above Table 4.11 shows that the ARIMA (1,1,2) model has ARCH effect, hence we have the evidence to perform the ARCH family of model for capturing the volatility of exchange rate returns.

#### 4.6 Forecasting Analysis

Forecasting performance of the fitted ARIMA(3,1, 2) model of exchange rate returns is examined through Mean Absolute Error (MAE), Root Mean Square Error (RMSE), Mean Absolute Percent Error (MAPE), and Theil inequality coefficient. The results are shown in Table. 4.12

Graph: 4.3 Forecast comparisons of Monthly Exchange Rate with actual Monthly Exchange rate data.

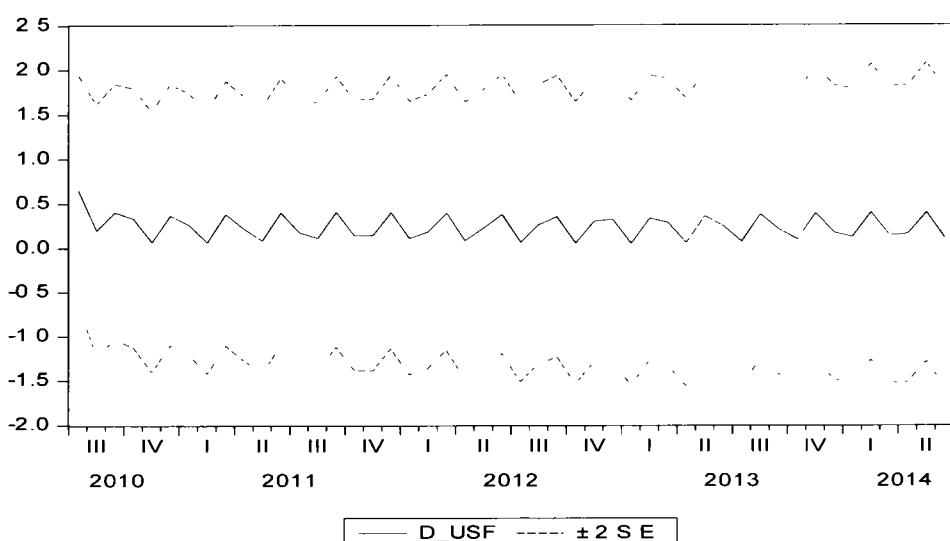


**Table 4.12** Forecasting Performance of Monthly and yearly Exchange Rate.

	<b>ARIMA(3,1,2) MONTHLY EXCHANGE RATE DATA</b>	<b>ARIMA (1,1,2) YEARLY EXCHANGE RATE DATA</b>
RMSE	1.190930	1.632320
MAE	0.745808	0.454367
MAPE	172.6314	182.8976
Theil Inequality Coefficient	0.0780373	0.076897
Bias Proportion	0.000856	0.000745
Variance Proportion	0.082410	0.467589
Covariance Proportion	0.775037	0.237845

The value of Theil inequality is 0.076897 indicating the model is a better fit. The bias proportion and variance proportion are close to zero. We can say that this model is good for forecasting purpose along with capturing the volatility

Graph: 4.4. Forecasting Graph of Monthly Exchange rate from 2010 to 2014



For checking forecasting performance of ARIMA (3,1,2) model. We forecast for the period of July, 2010 to June, 2014 the forecasting of Exchange Rate returns is between plus and minus 2 Standard deviation.

This research motivations on building a model for the exchange rate of Pakistan using time series methodology, Autoregressive (AR), Moving Average (MA) and Autoregressive Integrated Moving Average (ARIMA) for the selection of best fitted model we have choose the Akaike info criterion (AIC). The small value of AIC shows the better estimation. We have selected three best fitted models amongst AR, MA and ARIMA. AR (1) is 1.9697, MA (3) is 1.9583 and ARIMA (3,1,2) is 1.9516. Hence, here the best fitted model is ARIMA (3,1,2). The performance of forecast is measured by RMSE, MAE, MAPE and Thiel Inequality.

#### 4.7 Autoregressive Conditional Heteroscedasticity Model

**Table 4.13** ARCH model on ARIMA (3,1,2)

Model	AIC	SIC	Serial correlation test
1	1.969714	1.282960	Accept H0
2	0.942117	1.033294	Reject H0
3	1.267981	1.369288	Reject H0
4	1.099763	1.211201	Reject H0
5	1.268648	1.390217	Reject H0
6	1.245182	1.376882	Reject H0
7	1.321264	1.463095	Reject H0
8	1.296858	1.448820	Reject H0
9	1.325635	1.487728	Reject H0

Accept H<sub>0</sub> means there is no serial correlation

Table 4.13 shows the different ARCH models for checking the serial correlation we performed LM test. For selection of best model we used AIC and SIC criterions.

#### 4.8 Generalized Autoregressive Conditional Heteroscedasticity Model

**Table 4.14** GARCH model on ARIMA (3,1,2)

Model	AIC	SIC	Serial Correlation Test
1,1	1.272734	1.363911	Accept H0
1,2	1.116379	1.217686	Accept H0
1,3	1.041951	1.153390	Accept H0
1,4	1.254303	1.375872	Accept H0
1,5	1.346488	1.478188	Reject H0
1,6	1.107776	1.249606	Reject H0
1,7	1.047357	1.199318	Accept H0
1,8	1.034944	1.197036	Accept H0
1,9	1.276233	1.448456	Accept H0
2,1	0.961197	1.062504	Accept H0
2,2	0.875452	0.986891	Accept H0
2,3	0.999345	1.120914	Accept H0
2,4	1.052511	1.184211	Reject H0
2,5	1.037497	1.179328	Reject H0
2,6	1.034056	1.186018	Reject H0
2,7	0.927956	1.090048	Reject H0
2,8	0.880974	1.053198	Reject H0
2,9	0.946956	1.129310	Reject H0
3,1	0.980607	1.092046	Reject H0
3,2	0.998848	1.120417	Accept H0
3,3	0.954946	1.086646	Reject H0
3,4	0.996172	1.138002	Reject H0
3,5	1.027689	1.179650	Accept H0
3,6	1.054789	1.216882	Accept H0
3,7	0.970194	1.142417	Reject H0
3,8	0.988467	1.170821	Reject H0
3,9	0.918412	1.110897	Reject H0
4,1	1.270797	1.392366	Reject H0
4,2	1.290103	1.421803	Reject H0
4,3	1.292217	1.434047	Reject H0

Accept H<sub>0</sub> means there is no serial correlation

Table 4.14 shows the different combination of GARCH models for checking the serial correlation we performed LM test. For selection of best model we used AIC and SIC criterions.

## 4.9 Integrated Generalized Autoregressive Conditional Heteroscedasticity Model

**Table 4.15** IGARCH model on ARIMA (3,1,2)

Model	AIC	SIC	Serial Correlation Test
1,1	1.409964	1.480879	Reject H0
1,2	1.400527	1.481573	Reject H0
1,3	1.343087	1.434264	Reject H0
1,6	1.204152	1.325722	Reject H0
1,7	1.328376	1.460076	Reject H0
1,8	1.272177	1.414008	Accept H0
1,9	1.145223	1.297184	Reject H0
<b>2,1</b>	<b>1.049914</b>	<b>1.130960</b>	<b>Accept H0</b>
2,2	1.558736	1.649913	Reject H0
2,3	1.147756	1.249064	Reject H0
2,4	1.362550	1.473989	Reject H0
2,5	1.231142	1.352711	Reject H0
2,6	1.177189	1.308889	Reject H0
2,7	1.257310	1.399140	Reject H0
2,8	1.467310	1.297310	Reject H0
2,9	1.662550	1.862560	Reject H0
3,1	1.084078	1.175254	Accept H0
3,2	1.085565	1.186872	Accept H0
3,3	1.078014	1.189453	Accept H0
3,4	1.214523	1.336092	Accept H0
3,5	1.215488	1.347188	Reject H0
3,6	1.130056	1.271887	Reject H0
3,7	1.274305	1.426267	Reject H0
3,8	1.330552	1.492644	Reject H0
3,9	1.178999	1.351222	Reject H0
4,1	1.087995	1.189303	Accept H0
4,2	1.110229	1.221667	Accept H0
4,3	1.126037	1.247606	Accept H0
4,4	1.144590	1.276290	Accept H0
4,5	1.377709	1.519540	Reject H0
4,6	1.171164	1.323126	Reject H0
4,7	1.242775	1.404867	Reject H0

Accept  $H_0$  means there is no serial correlation

Table 4.15 shows the different combination of IGARCH models for checking the serial correlation we performed LM test. For selection of best model we used AIC and SIC criterions.

#### 4.10 Exponential Generalized Autoregressive Conditional Heteroscedasticity Model

**Table 4.16** EGARCH model on ARIMA (3,1,2)

Model	AIC	SIC	Serial Correlation Test
1,1	0.758053	1.049361	Accept H0
1,2	0.967384	1.078822	Reject H0
1,3	0.947586	1.069156	Reject H0
1,4	1.014194	1.145894	Reject H0
1,5	0.862117	1.003948	Reject H0
1,6	0.954958	1.106920	Reject H0
1,7	0.962414	1.113994	Reject H0
1,8	0.896211	1.343943	Reject H0
1,9	0.762227	1.983998	Reject H0
2,1	1.252803	1.364242	Reject H0
2,2	0.774738	0.896307	Accept H0
2,3	0.922264	1.053964	Reject H0
2,4	0.906392	1.048223	Reject H0
2,5	0.893471	1.045432	Reject H0
2,6	0.967922	1.004829	Reject H0
2,7	0.926294	1.068541	Reject H0
2,8	0.816639	0.948445	Reject H0
2,9	0.866981	0.108431	Reject H0
3,1	0.804055	0.925624	Accept H0
3,2	0.806731	0.938431	Reject H0
3,3	0.820609	0.962440	Reject H0

Accept H<sub>0</sub> means there is no serial correlation

Table 4.16 shows the different combination of EGARCH models for checking the serial correlation we performed LM test. For selection of best model we used AIC and SIC criterions. We have selected EGARCH (1,1) model for capturing the volatility of Exchange Rate data monthly as well as yearly.

#### 4.11 Best Fitted Model

**Table: 4.17 ARIMA (3,1,2) EGARCH(1,1),Mean Equation, Monthly Exchange Rate**

Variable	Coefficient	Std. Error	z-Statistic	Prob.
C	0.069188	0.031986	2.163087	0.0305
AR(1)	0.552573	0.060463	9.139087	0.0000
AR(2)	0.900300	0.009851	91.38798	0.0000
AR(3)	-0.472570	0.057128	-8.272202	0.0000
MA(1)	0.002813	0.003173	0.886554	0.3753
MA(2)	-0.976045	0.002756	-354.1375	0.0000

**Table: 4.18 ARIMA (3,1,2) EGARCH(1,1),Variance Equation, Monthly Exchange Rate**

Variable	Coefficient	Std. Error	z-Statistic	Prob.
C(7)	-0.461995	0.034727	-13.30381	0.0000
C(8)	0.535711	0.053967	9.926641	0.0000
C(9)	0.302832	0.044388	6.822409	0.0000
C(10)	0.953808	0.009531	100.0706	0.0000

$$LN(GARCH) = -0.4619 + 0.5357ABS(RESID(-1)/@SQRT(GARCH(-1))) + 0.3028$$

$$RESID(-1)/@SQRT(GARCH(-1)) + 0.9538LN(GARCH(-1))$$

EGARCH parameters, displayed in Table 4.17 and Table 4.18 shows mean equation variables of EGARCH (1,1) model, the calculated coefficients and the p' values of the EGARCH model on monthly exchange rate returns also presented. The results shows that, there is a first order autoregressive behavior in the exchange rate as in the mean equation, as all the Autoregressive and Moving averages lag are significant at 1% in monthly exchange rate returns. The constant C is also significant at 5% in monthly exchange rate returns. In the variance equation, all the terms are significance at 1% level for the monthly exchange rate returns. The EGARCH model proves to be the best model to explain the behavior of exchange rate monthly data as the most of the coefficients of mean and variance equation are significant.

**Table: 4.19 ARIMA (1,1,2) EGARCH(1,1)Mean Equation yearly Exchange Rate**

Variable	Coefficient	Std. Error	z-Statistic	Prob.
C	3.525186	1.587157	2.221069	0.0263
AR(1)	0.911973	0.104118	8.759007	0.0000
MA(1)	-0.610614	0.186334	-3.276985	0.0010
MA(2)	-0.315140	0.198853	-2.584793	0.0130

**Table: 4.20 ARIMA (1,1,2) EGARCH(1,1)Variance Equation yearly Exchange Rate**

Variable	Coefficient	Std. Error	z-Statistic	Prob.
C(5)	0.331116	0.517818	2.639445	0.0425
C(6)	-0.272655	0.769568	-1.354297	0.0231
C(7)	0.106108	0.206847	3.512978	0.0080
C(8)	1.022685	0.154416	6.622931	0.0000

$$LN(GARCH) = 0.3311 - 0.2726ABS(RESID(-1)/@SQRT(GARCH(-1))) + 0.1061$$

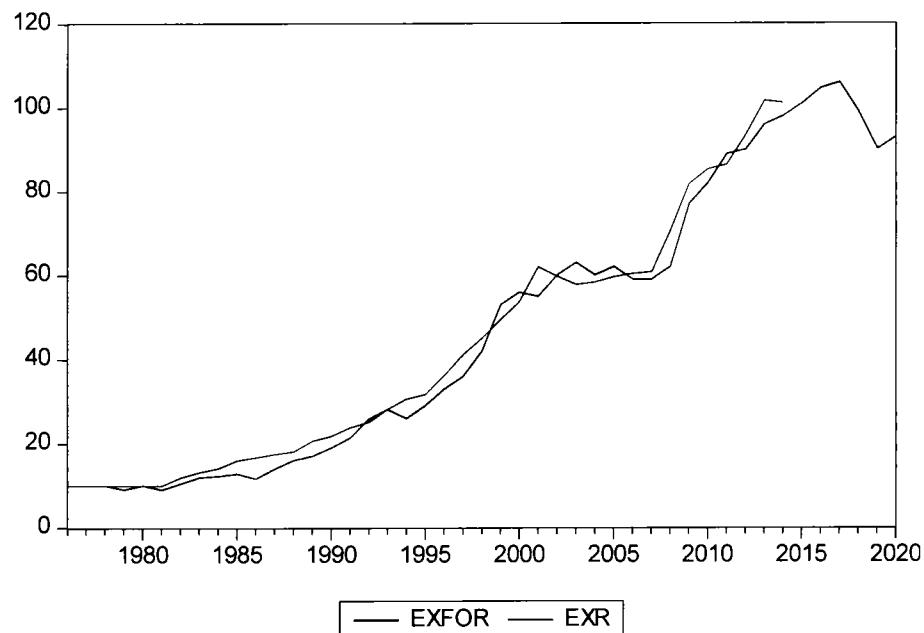
$$RESID(-1)/@SQRT(GARCH(-1)) + 1.0226LN(GARCH(-1))$$

EGARCH parameters, displayed in Table 4.19 and Table 4.20 shows mean equation variables of EGARCH (1,1) model, the calculated coefficients and the p' values of the EGARCH model on yearly exchange rate returns also presented. The results shows that, there is a first order autoregressive behavior in the exchange rate as in the mean equation, as all the Autoregressive and Moving averages lag are significant at 1% in yearly exchange rate returns. The constant C is also significant at 5% in yearly exchange rate returns. In the variance equation, C(7) and C(8) terms are significance at 1% level and C(5) and C(6) are significant at 5% level for yearly exchange rate returns. The EGARCH model proves to be the best model to explain the behavior of exchange rate yearly data as the most of the coefficients of mean and variance equation are significant.

## 4.12 Forecasting Analysis

Forecasting performance of the fitted EGARCH (1,1) model of exchange rate returns is examined through Mean Absolute Error (MAE), Root Mean Square Error (RMSE), Mean Absolute Percent Error (MAPE), and Theil inequality coefficient. The results are shown in Table 4.14.

Graph: 4.5 Yearly Exchange Rate



Graph: 4.6 Monthly Exchange Rate

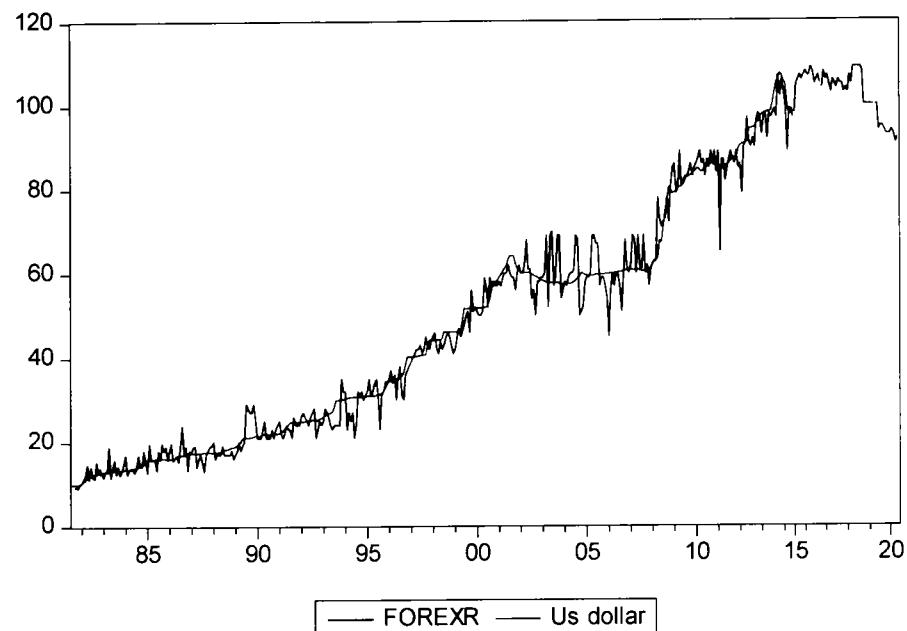


Table: 4.21 Forecast Performance

	EGARCH(1,1) MONTHLY EXCHANGE RATE DATA	EGARCH (1,1) YEARLY EXCHANGE RATE DATA
RMSE	0.818931	0.732360
MAE	0.765453	0.352010
MAPE	198.6314	174.7645
Theil Inequality Coefficient		
Bias Proportion	0.000467	0.003324
Variance Proportion	0.072470	0.851989
Covariance Proportion	0.805037	0.884714

The value of Theil inequality is 0.060137 indicating the model is a better fit. The bias proportion and variance proportion are close to zero. We can say that this model is good for forecasting purpose along with capturing the volatility

#### 4.13 VECTOR AUTOREGRESSIVE MODEL RESULTS

All the variables are stationary at first difference Augmented Dickey Fuller test has been used for the unit root test. The said test verified at level all variables are non-stationary after taking the first difference became stationary at 1% level of significance the earlier table shows that studied variables are stationary I(1).

**Table 4.22** VAR Lag Selection Criteria

Lag	LogL	LR	FPE	AIC	SC	HQ
0	-78.86196	NA	9.62e-06	5.474965	5.752511	5.565438
1	133.5104	328.8346*	1.15e10*	-5.903895	3.961074*	5.270584*
2	171.2754	43.85616	1.37e-10	-6.017768	-2.409671	-4.841618
3	220.5658	38.16028	1.39e-10	6.875211*	-1.601839	-5.156223

\* indicates lag order selected by the criterion

The basic step before using appropriate Vector Autoregressive model is the suitable lag selection for the variables. For the selection of suitable lag length there are many criterions for lag length LR sequential modified LR test statistic (each test at 5% level), FPE Final prediction error, AIC Akaike information criterion, SC Schwarz information criterion and HQ Hannan-Quinn information criterion. The study used one optimal lag because from all six criterions five are favor one lag.

Table:4.23 Vector Auto regression Estimates

DEPENDENT	LGDPR	LEXR	LNEXPP	FDI	INF	LREM
INDEPENDENT	LGDPR(-1)	LEXR(-1)	LNEXPP(-1)	FDI(-1)	INF(-1)	LREM(-1)
	0.826657 (0.08438) [ 9.79650]	0.726911 (0.26247) [ 2.76949]	0.107789 (0.66732) [ 0.16153]	1.679118 (2.28145) [ 0.73599]	24.99964 (14.8064) [ 1.6844]	-2.864176 (1.25409) [ -2.2838]
	LEXR(-1)	0.034582 (0.03774) [ 0.91629]	0.699185 (0.11739) [ 5.95598]	0.088944 (0.29846) [ 0.29801]	-1.459993 (1.02040) [ -1.43081]	-19.24141 (6.62225) [ -2.90557]
	LNEXPP(-1)	0.049496 (0.02211) [ 2.23894]	-0.202985 (0.06876) [ -2.95196]	0.717645 (0.17482) [ 4.10494]	1.578861 (0.59770) [ 2.64156]	5.267510 (3.87900) [ 1.35795]
	FDI(-1)	0.009595 (0.00612) [ 1.56664]	-0.010789 (0.01905) [ -0.56632]	0.032671 (0.04843) [ 0.67455]	0.529452 (0.16559) [ 3.19738]	0.149590 (1.07466) [ 0.13920]
	INF(-1)	-0.002112 (0.00081) [ -2.61936]	0.005327 (0.00251) [ 2.12460]	-0.007167 (0.00638) [ -1.12423]	-0.048275 (0.02180) [ -2.21496]	0.205955 (0.14145) [ 1.45604]
						[- 0.00820]
	LREM(-1)	0.017347 (0.00533) [ 3.25701]	-0.038153 (0.01657) [ -2.30297]	0.000480 (0.04212) [ 0.01140]	-0.109544 (0.14400) [ -0.76071]	-0.563315 (0.93455) [ -0.60277]
	C	1.759352 (0.96603) [ 1.82121]	-7.039680 (3.00482) [ -2.34279]	1.681186 (7.63956) [ 0.22006]	-37.38749 (26.1185) [ -1.43145]	-376.5015 (169.506) [ -2.22117]
	R-squared	0.999215	0.996727	0.969974	0.936160	0.683560
	Adj. R-squared	0.999034	0.995971	0.963045	0.921428	0.610535
	F-statistic & Prob	5516.221 (0.0000)	1319.498 (0.0000)	139.9873 (0.0000)	63.54498 (0.0000)	9.360658 (0.0000)

The results of the unrestricted VAR model are showed in Table 4.23, Considered Real Gross Domestic Product (GDP) equation (1<sup>st</sup> Column of Table 4.23 ). We have six dependent variable, Inflation Rate (INF), foreign direct investment (FDI), Exports, Real GDP and foreign remittances and Exchange Rate of Pakistan. We have Chosen one lag with the guidance of lag selection criterions, so, there are one lag for each model and constant for this model. We have six dependent variable and every variable have seven independent variable, so; total 42 coefficients have in this VAR model. Now for

checking the significance we need P-value. The guideline is if P-value is less than 5% than the variable has significant impact on endogenous variable.

**Table: 4.24** Coefficients of VAR model

	Coefficient	Std. Error	t-Statistic	Prob.
C(1)	0.826657	0.084383	9.796498	0.0000
C(2)	0.034582	0.037741	0.916292	0.3609
C(3)	0.049496	0.022107	2.238942	0.0266
C(4)	0.009595	0.006125	1.566644	0.1192
C(5)	-0.002112	0.000806	-2.619363	0.0097
C(6)	0.017347	0.005326	3.257009	0.0014
C(7)	1.759352	0.966033	1.821214	0.0705
C(8)	0.726911	0.262471	2.769488	0.0063
C(9)	0.699185	0.117392	5.955977	0.0000
C(10)	-0.202985	0.068763	-2.951956	0.0036
C(11)	-0.010789	0.019050	-0.566322	0.5720
C(12)	0.005327	0.002507	2.124603	0.0352
C(13)	-0.038153	0.016567	-2.302970	0.0226
C(14)	-7.039680	3.004823	-2.342794	0.0204
C(15)	0.107789	0.667316	0.161526	0.8719
C(16)	0.088944	0.298462	0.298007	0.7661
C(17)	0.717645	0.174825	4.104935	0.0001
C(18)	0.032671	0.048434	0.674548	0.5010
C(19)	-0.007167	0.006375	-1.124230	0.2626
C(20)	0.000480	0.042120	0.011403	0.9909
C(21)	1.681186	7.639563	0.220063	0.8261
C(22)	1.679118	2.281452	0.735986	0.4628
C(23)	-1.459993	1.020396	-1.430810	0.1545
C(24)	1.578861	0.597700	2.641561	0.0091
C(25)	0.529452	0.165590	3.197376	0.0017
C(26)	-0.048275	0.021795	-2.214958	0.0282
C(27)	-0.109544	0.144001	-0.760714	0.4480
C(28)	-37.38749	26.11853	-1.431455	0.1543
C(29)	24.99964	14.80635	1.688440	0.0933
C(30)	-19.24141	6.622249	-2.905570	0.0042
C(31)	5.267510	3.879003	1.357955	0.1764
C(32)	0.149590	1.074656	0.139198	0.8895
C(33)	0.205955	0.141448	1.456045	0.1474
C(34)	-0.563315	0.934550	-0.602767	0.5475
C(35)	-376.5015	169.5061	-2.221168	0.0278
C(36)	-2.864176	1.254086	-2.283875	0.0237
C(37)	1.454900	0.560899	2.593870	0.0104
C(38)	0.238525	0.328548	0.725996	0.4689
C(39)	0.151905	0.091023	1.668875	0.0971
C(40)	-9.82E-05	0.011981	-0.008200	0.9935
C(41)	1.108143	0.079156	13.99955	0.0000
C(42)	34.05446	14.35703	2.371970	0.0189

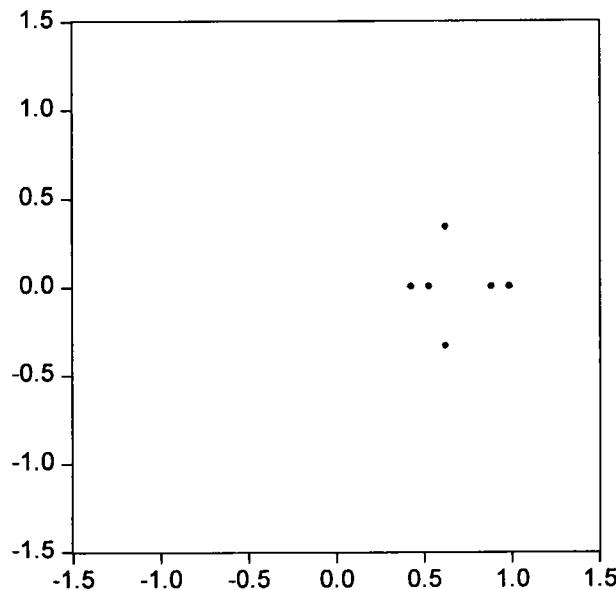
R-squared	0.999215	Mean dependent var	15.47185
Adjusted R-squared	0.999034	S.D. dependent var	0.434494
S.E. of regression	0.013505	Sum squared resid	0.004742

$$\begin{aligned}
 LGDPR = & 1.759352 + 0.826657 LGDPR(-1) + 0.034582 LEXR(-1) + 0.049496 LNEXPP(-1) + \\
 & 0.009595 LFDI(-1) + -0.002112 INF(-1) + 0.017347 LREM(-1)
 \end{aligned}$$

Exchange rate has no significant impact on variability of Real Gross Domestic Product (GDP) in the Pakistan. Lag of GDP has significant impact on Real GDP similarly inflation rate and foreign remittances have significantly affect Real GDP of Pakistan.

#### Graph: 4.7 AR Roots Graph

Inverse Roots of AR Characteristic Polynomial



AR Roots Graph shows the inverse roots of the characteristic AR polynomial. The above graph shows that estimated VAR is stable (stationary) because all roots have modulus lie inside the unit circle so result are valid.

#### 4.14 VARIANCE DECOMPOSITION ANALYSIS:

There are two methods variance decomposition analysis and impulse response function to expand investigation and study of the effects of shocks to Gross Domestic Product (GDP). Variance Decomposition functions as a tool for assessing dynamic relations and strengths of causal relations among variables in the system. Below table 4.26 depict the results of the variance Decomposition, they are presenting that there are significant role played by the shocks in Exchange rate in accounting for the variability in the Gross Domestic Product (GDP) in Pakistan.

**Table No. 4.25** Variance decomposition of Real GDP.

Period	S.E.	LGDPR	LEXR	LNEXPP	LFDI	INF	LREM
1	0.013505	100.0000	0.000000	0.000000	0.000000	0.000000	0.000000
2	0.020011	83.59865	2.427145	4.215583	2.400988	5.135455	2.222182
3	0.025494	67.32039	2.639610	9.425471	6.012614	8.454782	6.147137
4	0.029951	55.89060	1.957701	12.87170	9.559972	9.327901	10.39212
5	0.033546	48.17350	1.846611	14.30930	12.52045	8.924453	14.22569
6	0.036523	42.82195	2.635304	14.36258	14.73310	8.098626	17.34844
7	0.039076	38.98446	3.987754	13.73342	16.26775	7.264912	19.76170
8	0.041325	36.15880	5.454020	12.89705	17.30483	6.557559	21.62774
9	0.043348	34.01886	6.746561	12.08347	18.02825	5.984748	23.13811
10	0.045205	32.32902	7.766846	11.37049	18.57318	5.519000	24.44147

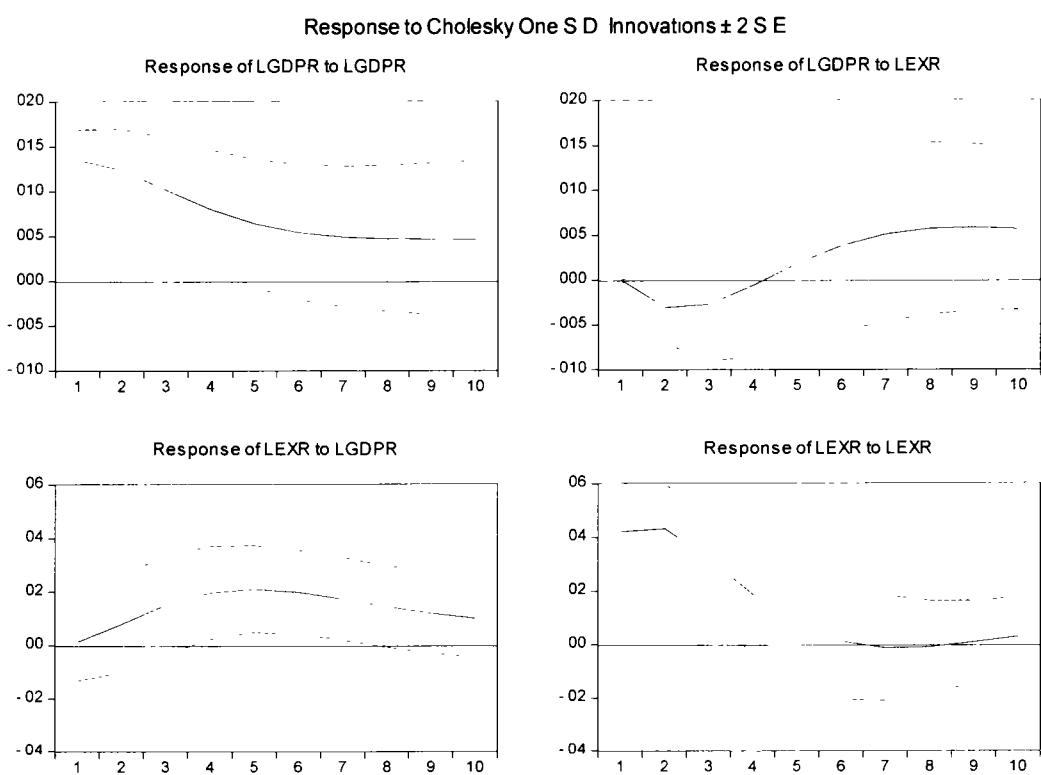
The result shows that in short run impulse of innovation of shock to Real GDP account for 67.32% variation of the fluctuation in Real GDP (own shock) and in long run i.e. 10 years is 32.32% variation of the fluctuation in Real GDP (own shocks). Shock to Exchange rate can cause 2.63% in short run but contribution in long run is 7.76% to the Real GDP in Pakistan.

#### 4.15 Impulse Response Function:

The Impulse response function is a shock to a VAR system. The Impulse responses identify the responsiveness of the dependent variable (Endogenous variable) in the VAR when a shock is put to the error term.

The impulse response graphs indicate that response of Real Gross Domestic Product to one standard deviation shock in Exchange Rate of Pakistan initially during the first four years decline and negative effect rising subsequently in the direction of the equilibrium level in the fifth year of the forecast period. Real GDP is increasing steadily through the last five year in response of shock to Exchange rate.

Graph: 4.8 Impulse response function



## **Chapter 5**

### **Conclusion**

This research motivation on building a model for the exchange rate volatility of Pakistan using time series methodology. As the monetary time series like exchange rate may have volatility, an effort is made to model this volatility using ARCH family of models. Increasing role of exchange rate in corporate decision making is becoming famous in the emerging economies. Exchange rate volatility occupied a significant position all over the world in Investment decision. Exchange rate volatility is equally helpful in many micro as well as macro-economic decision-making. Monthly as well as yearly foreign exchange rates of Pakistan for the period ranging from July 1981 to May 2014 are used for this purpose. The stationarity of the exchange rate returns is inspected through graphical analysis, Augmented Dicky Fuller test and correlogram which showed the series is nonstationary at level but after taking first difference it became stationary. For selection of mean model we have used Autoregressive (AR), Moving Average (MA) and Autoregressive Integrated Moving Average (ARIMA). ARIMA (3,1,2) and ARIMA (1,1,2) selected appropriate models for monthly and yearly Exchange rate data, respectively. We have performed forecast from 1981 to 2014 as well as 2010 to 2014 with the help of these selected models. The performance of forecast was evaluated by RMSE (Root Mean Square Error), MAE (Mean Absolute Error), MAPE (Mean Absolute Percentage Error) and Theil's Inequality coefficient. The ARCH-LM test and residual of ARIMA (3,1,2) and ARIMA (1,1,2) have justified to run ARCH family of models. We have used the different sets of ARCH, GARCH, EGARCH, and IGARCH.

The diagnostic checking has shown that for monthly exchange rate data the ARIMA(3,1,2)-EGARCH (1,1) and for yearly exchange rate data the ARIMA(1,1,2)-EGARCH(1,1) are the best fitted models for modeling and forecasting Exchange Rate volatility. We have made forecast from 1981 to 2020 with these models. The performance of forecast was evaluated by RMSE (Root Mean Square Error), MAE (Mean Absolute Error), MAPE (Mean Absolute Percentage Error) and Theil's Inequality coefficient. These forecasts would be helpful for the policy makers to foresee the future requirements.

On second part the study examined the impact of exchange rate volatility on Pakistan's economy using yearly data from 1981 to 2014. The finding of this study showed significant impact of exchange rate on Real Gross Domestic Product of Pakistan. The study has used six variables i.e. the data for the variables i.e. Exchange Rate, inflation Rate (INF), foreign direct investment (FDI), Exports, Real GDP and foreign remittances obtained from The State Bank of Pakistan. The empirical relationship between exchange rate volatility and Real Gross Domestic Product (GDP) have been found while employing an econometric study based on Vector Autoregressive (VAR) methodology. We have chosen one lag by the guidance of different lag selection criterions. The result of VAR model shows Exchange rate volatility has significant impact on variability of Real Gross Domestic Product (GDP) in the Pakistan and lag of Real GDP has significant impact on Real GDP. Similarly inflation rate and foreign remittances have significant effect on Real GDP of Pakistan. AR Roots Graph showed estimated VAR is stable (stationary) because all roots have modulus lie inside the unit circle so result are valid. Study shows that in short run impulse of innovation of shock to Real GDP account for 67.32% variation of the fluctuation in Real GDP (own shock) and in long run i.e. 10

years is 32.32% variation of the fluctuation in Real GDP (own shocks). Shock to Exchange rate can cause 2.63% in short run but contribution in long run is 7.76% to the Real GDP in Pakistan. The impulse response graphs indicate that response of Real Gross Domestic Product to one standard deviation shock in Exchange Rate of Pakistan initially during the first four years decline and negative effect rising subsequently in the direction of the equilibrium level in the fifth year of the forecast period. Real GDP is increasing steadily through the last five year in response of shock to Exchange rate.

## Chapter 6

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